## Processing and analyzing the GW150914 data and their possible physical interpretations Plamen Fiziev Sofia University Foundation TCPA & BLTF, JINR, Dubna BAN, Sofia, 11 April 2016



## The Universe as seen in different wave lengths



## Plan of the talk:

- 1. History and basics of theory of GW.
- 2. First indications for existence of GW: Huls-Taylor (1993).
- 3. The development of Numerical Relativity.
- 4. GW150914 announcement and its announced features.
- 5. The real data for GW150914 and their analysis.
- 6. The problems with QNM analysis.
- 7. Possible alternative explanations and models of GW150914 and their problems.
- 10. Some basic conclusions.

The existence of gravitational waves (GW) was hypothesized on the basis of general considerations for the first time by Oliver Heaviside (1893) (in his book *Electromagnetic theory*),

and independently by

Hendric A. Lorentz (1900),

and by

Henri Poincare (1905).

Leading idea: finite velocity of spreading of

Electromagnet interaction in vacuum:



No specific theory of GW was proposed at that time, or at least is not known.





**Oliver Heaviside** 

Hendric A. Lorentz

Henri Poincare



GW were predicted in 1916 by Albert Einstein to exist on the basis of his theory of general relativity, gravitational waves theoretically transport energy as gravitational radiation.



Albert Einstein: First theory of GW – 1916-18 A. Einstein, Sitzungsber. preuss. Akad. Wiss.,B. 1916, S. 688; 1918, S. 154.

Remember that the basic PHYSICAL Einsten's idea for inventing GR was also the finite speed of spreading of gravity! The geometry was only a tool!

## Weak field approximation in GR

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}, \quad h_{\mu\nu} \ll 1. \qquad h_{\mu\nu}(x,t) = \frac{4G}{c^2} \int \frac{S_{\mu\nu}(x',t-\frac{|x-x'|}{c})}{|x-x'|} d^3x'$$
$$S_{\mu\nu} = T_{\mu\nu} - 1/2 g_{\mu\nu} T^{\lambda}_{\lambda}$$

Flat waves: 
$$h_{\mu\nu} = \varepsilon_{\mu\nu} \exp(ik_{\lambda}x^{\lambda}) + \varepsilon^*_{\mu\nu} \exp(-ik\lambda x^{\lambda}).$$

Wave equation:  $k^{\mu}k_{\mu} =$ 

$$\kappa \kappa_{\mu} \equiv 0$$

0

Gauge transformations:  $x'^{\mu} = x^{\mu} + \xi^{\mu}(x).$  Harmonic gauge:  $k_{\mu}\varepsilon^{\mu}{}_{\nu} = 1/2 k_{\nu}\varepsilon^{\mu}{}_{\mu}$   $\varepsilon_{\mu\nu} = \varepsilon_{\nu\mu}$  $h'_{\mu\nu} = h_{\mu\nu} - \xi_{\mu,\nu} - \xi_{\nu,\mu}$  $\varepsilon'_{\mu\nu} = \varepsilon_{\mu\nu} + k_{\mu}e_{\nu} + k_{\nu}e_{\mu}$ .  $\xi^{\mu}(x) = i e_{\mu}e^{ikx} - i e_{\mu}^{*}e^{-ikx}$ 

Flat GW along axes Oz:

$$k^3 = k^0 \equiv k(>0), \quad k^1 = k^2 = 0.$$

Rotation around axes Oz:  

$$R(\theta) = \begin{pmatrix} \cos \theta & \sin \theta & 0 \\ -\sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \implies$$

$$h_{\mu\nu} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & h_{11} & h_{12} & 0 \\ 0 & h_{12} & -h_{11} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

only the two states  $\varepsilon_{11} \pm i\varepsilon_{12}$  exist, with  $J_z = \pm 2$ 

The graviton is particle with spin 2  $\varepsilon_{11}' - i\varepsilon_{12}' = e^{2i\theta}(\varepsilon_{11} - i\varepsilon_{12})$ 

# The two types of GW in GR:

 $V_{GW}$  = c



$$h = 2\frac{\delta \ell}{\ell}.$$

Polarization of GW in modified theories of gravity (f(R), MDG, Hordensky model...)



Figure 4: Effect of the six possible GW polarization modes on a ring of test particles. The GW propagates in the z-direction for the upper three transverse modes, and in the x-direction for the lower three longitudinal modes. Only modes (a) and (b) are possible in GR. Image reproduced by permission from [471].

## Quadrupole character of GW (NASA Goddard)



## First indirect evidences for gravitational waves

 $r^{5}$ 

5

 $48\pi (GM)$ 

 $32 G^4 (m_1 m_2)^2 (m_1 + m_2)$ 





 $2.422 \pm 0.006) \times 10^{-12}$ 

 $\frac{\mathrm{d}\tau}{\mathrm{d}t}$ 





## Indirect detection of gravitational waves 1993 Nobel Price: Hulst &Taylor



# BH merger:

The collision of two BH will produce a ringing single final BH (Stephen Hawking,+...)

From the ring-down waves we can infer the mass, the spin and surface area of the final BH.

Kip Thorne, in The Future of Theoretical Physics and Cosmology, Cambridge, 2003:



"If the total area does not increase, Stephen is wrong, Einstein's GR laws are wrong, and we will have a great crisis in physics... Since the 1970's these remarkable predictions have remained untested. They seem to be an unequivocal consequence of Einstein's GR laws,

but relativity might be wrong or (much less likely) we might be misinterpreting its mathematics."

## BH merger (NR)

Phase transitions

## Several Orbits: NR is not what it was!



Figure: Success after 30 years: 4.2 Orbits and waveforms, NASA Goddard.

Radiated energy: 3.6 - 3.9%, final  $a/M \approx 0.7$ .

Palma de Mallorca 07/09/06

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**NR Problems:** 1. We have No resolution of the GR constraints. 2. Superluminal Signals and waves. 3. Singularities are not resolved but just put under carpet. 4. Too expensive and CPU time consuming  $\Rightarrow$  only a few exact NR waveforms are available.

5. Works only for restricted domain of BH masses
6. Eccentricity and spin effects for higher GW modes, are not taken into account.

#### Rainer Weis, NSF Director France A. Córdova, David Reitze, Gabriela Gonzalez, Kip Thorn



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### Basic announced results according PRL 116, 061102 (2016)



## GW150914:FACTSHEET

BACKGROUND IMAGES: TIME-FREQUENCY TRACE (TOP) AND TIME-SERIES (BOTTOM) IN THE TWO LIGO DETECTORS; SIMULATION OF BLACK HOLE HORIZONS (MIDDLE-TOP), BEST FIT WAVEFORM (MIDDLE-BOTTOM)

#### first direct detection of gravitational waves (GW) and first direct observation of a black hole binary

observed by	LIGO L1, H1	duration from 30 Hz	~ 200 ms		
source type	black hole (BH) binary	# cycles from 30 Hz	~10		
date	14 Sept 2015	peak GW strain	1 x 10 <sup>-21</sup>		
time	09:50:45 UTC	peak displacement of	+0.002 fm		
likely distance	0.75 to 1.9 Gly 230 to 570 Mpc	interferometers arms frequency/wavelength	150 Hz, 2000 km		
redshift	0.054 to 0.136	at peak GW strain	~ 0.6.c		
signal-to-noise ratio	(24)	peak GW luminosity	3.6 x 10 <sup>56</sup> erg s <sup>-1</sup>		
false alarm prob.	< 1 in 5 million	radiated GW energy	2.5-3.5 M⊙		
false alarm rate	< 1 in 200,000 yr	remnant ringdown fre	a. ~ 250 Hz		
Source Masses Mo		remnant damping time ~ 4 ms			
total mass primary BH secondary BH remnant BH	60 to 70 32 to 41 25 to 33 58 to 67	remnant size, area consistent with general relativity? graviton mass bound	180 km, 3.5 x 10 <sup>5</sup> km <sup>2</sup> passes all tests performed < 1.2 x 10 <sup>-22</sup> eV		
mass ratio primary BH spin	0.6 to 1 < 0.7	coalescence rate of binary black holes	2 to 400 Gpc <sup>-3</sup> yr <sup>-1</sup>		
secondary BH spin remnant BH spin	< 0.9 0.57 to 0.72	online trigger latency # offline analysis pipeli	~ 3 min nes 5		
signal arrival time delay	arrived in L1 7 ms before H1	CPU hours consumed	~ 50 million (=20,000 PCs run for 100 days)		
likely sky position likely orientation resolved to	Southern Hemisphere face-on/off ~600 sq. deg.	papers on Feb 11, 2016 <mark># res</mark> earchers	<ul> <li>13</li> <li>~1000, 80 institutions</li> <li>in 15 countries</li> </ul>		



Parameter ranges correspond to 90% credible bounds. Acronyms: L1=LIGO Livingston, H1=LIGO Hanford; Gly=giga lightyear=9.46  $\times 10^{12}$ km; Mpc=mega parsec=3.2 million lightyear,  $Gpc=10^3 Mpc$ , fm=femtometer=10-15 m, M⊙=1 solar mass= $2 \times 10^{30} \text{ kg}$ 

## Peak GW luminosity:

$$L_{mreging} = Mc^2/R_g/c \approx 3.6 \times 10^{56} \ erg/s$$

$$L_{Planck} = E_{Planck}/t_{Planck} = c^5/G \approx 10^{58} \ erg/s$$

### **Available Data for GW150914**

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← → X [] file:///D:/art/GW/LIGO%	20open/LIGO%20Open%20Science%20Center.html	<b>€</b> ₹	0	*	Ξ
👯 Apps 🗀 Journals 🗀 Fiziev 📑 Plamen Fizie	v F SquirrelMail - Login 👾 BLTP WebMail - Login 🕋 bng 👩 Google Hayka 峰 Google Translate 🗀 Ianl 👾 JINR LTP 👩 Google Scholar 🙆 АБВ Поща 💿 ECOST 📋 Импортирани от Inte	»	) Other	r bookn	narks
LIGO	LIGO is operated by California Institute of Technology and Massachusetts Institute of Technology and supported by the U.S. National Science Foundation.				
Getting Started	Data release for event GW150914				
Tutorials	This page has been prepared by the LIGO Scientific Collaboration (LSC) and the Virgo Collaboration to inform the broader				
Data & Catalogs	community about a confirmed astrophysical event observed by the gravitational-wave detectors, and to make the data around				
Timelines	that time available for others to analyze. There is also a <b>technical details</b> page about the data linked below, and feel free to <b>contact us.</b> This dataset has the Digital Object Identifier (doi) http://dx.doi.org/10.7935/K5MW2F23				

#### **Summary of Observation**

GPS ↔ UTCThe event occurred at GPS time 1126259462.39 == September 14 2015, 09:50:45.39 UTC. The false alarm rate is estimated<br/>to be less than 1 event per 203,000 years, equivalent to a significance of 5.1 sigma. The event was detected in data from<br/>the LIGO Hanford and LIGO Livingston observatories.

- There are Science Summaries, covering the information below in ordinary language.
- Acknowledgement There is a one page factsheet about GW150914, summarizing the event.

#### How to Use this Page

- Click on the section headings below to show available data files.
  - (click to Open/Close all sections)
- There are lots of data files available in the sections below, look for the word DATA.
- Click on each thumbnail image for larger image.

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My Sources

Student Projects

Software

#### University of Washington 22 February 2016

### David Shoemaker For the LIGO and Virgo Scientific Collaborations



Hanford

- Mission: to develop gravitational-wave detectors, and to operate them as astrophysical observatories
- Jointly managed by Caltech and MIT; LIGO Hanford and Livingston Observatories
- Requires instrument science at the frontiers of physics fundamental limits

MIT



Livingston

Caltech

## Measuring $\Delta L = 4 \times 10^{-18} m$



wave amplitude ( Strain  $\sim 10^{-22}$  )

#### David Shoemaker For the LIGO and Virgo Scientific Collaborations

- Requires the state of the art in substrates and polishing
- · Pushes the art for coating!
- Sum-nm flatness over 300mm





#### PHYSICAL REVIEW LETTERS

#### 12 FEBRUARY 2016



Parameter space of the initial bodies: a)  $m_{1,2}$  $S_{1,2}$ b) luminosity distance  $D_{\rm L}$ ascension  $\alpha$ declination  $\delta$ ) orbital inclination  $\iota$ polarization  $\psi$ ) time  $t_{\rm c}$ phase  $\phi_{\rm c}$  of coalescence. the eccentricity (two parameters)  $m = (1+z)m^{\text{source}}$ 

All together 17 parameters

There are not enough data to find all of them for GW150914!

## LIGO publications about GW150914 at LIGO side:

### **1. About the Instruments and Collaborations**

- 2. Observing Gravitational-Wave Transient GW150914 with Minimal Assumptions
- 3. GW150914: First Results from the Search for Binary Black Hole Coalescence with Advanced LIGO (PRL 116, 061102 (2016))
- 4. Properties of the binary black hole merger GW150914
- 5. The Rate of Binary Black Hole Mergers Inferred from Advanced LIGO Observations Surrounding GW150914
- 6. Astrophysical Implications of the Binary Black-Hole Merger GW150914
- 7. Tests of general relativity with GW150914
- 8. GW150914: Implications for the Stochastic Gravitational-Wave Background from Binary Black Holes
- 9. Calibration of the Advanced LIGO detectors for the discovery of the binary black-hole merger GW150914
- 10. Characterization of Transient Noise in Advanced LIGO Relevant to Gravitational Wave Signal GW150914
- 11. High-energy Neutrino Follow-up Search of Gravitational Wave Event GW150914 with IceCube and ANTARES
- 12. GW150914: The Advanced LIGO Detectors in the Era of First Discoveries
- 13. Localization and broadband follow-up of the gravitational-wave transient GW150914

## The real signal from GW150914 - Coherent Wave Burst (CWB)





2048 points, Corr\_Coeff (H5,L5) = -0.0458151661



## The GW150914 – CWB results:

The CWB pipeline searches for a broad range of GW transients in the LIGO frequency band **without prior knowledge of the signal waveforms**, and reconstructs the GW signal associated with these events using a likelihood analysis (arXiv:0802.3232 +...). Results for 2048 points:



2048 points, Corr\_Coeff (H4,L4) = -0.0512823348



GW150914 is not from cosmic strings or Supernovae, but from binary merger

## The Pearson correlation coefficient : definition and examples



$$\mathbf{r}_{\mathbf{x}\mathbf{y}} = \frac{\sum(\mathbf{x} - \bar{\mathbf{x}})(\mathbf{y} - \bar{\mathbf{y}})}{\sqrt{\sum(\mathbf{x} - \bar{\mathbf{x}})^2 \sum(\mathbf{y} - \bar{\mathbf{y}})^2}}$$



correlation

association

association

association

association

A measure of the strength and direction of the linear relationship between two variables that is defined as the (sample) covariance of the variables divided by the product of their (sample) standard deviations.

### The GW150914 – Observed WF (PRL 116, 061102 (2016) ):

Time series are filtered with a 35–350 Hz bandpass filter to suppress large fluctuations outside the detectors' most sensitive frequency band, and band-reject filters to remove the strong instrumental spectral lines



3441 points

Corr\_Coeff (H1,L1) = 0.28833 (too low ?)



### Properties of the binary black hole merger GW150914 :



Time-domain data (sampled at 2048 Hz) and reconstructed waveforms of GW150914, whitened by the noise power spectral density. In the Figure the data are band-passed and notched filtered. Shaded regions correspond to the 90% credible regions for the reconstructed waveforms.

### Properties of the binary black hole merger GW150914:



#### **Initial masses distributions:**

Overall (solid black), IMRPhenom (blue) and EOBNR (red) PDFs;

The dashed vertical lines mark the 90% credible interval for the Overall PDF.

The 2-dimensional plot shows the contours of the 50% and 90% credible regions plotted over a colour-coded posterior density function.



Source-frame mass and spin of the remnant BH produced by the coalescence of the binary. In the 1-dimensional marginalised distributions we show the Overall (solid black), IMRPhenom (blue) and EOBNR (red) PDFs; the dashed vertical lines mark the 90% credible interval for the Overall PDF. The 2-dimensional plot shows the contours of the 50% and 90% credible regions plotted over a colour-coded PDF.

#### 12 FEBRUARY 2016

### PHYSICAL REVIEW LETTERS



arXiv:1602.06833, A. Torres-Forn'e, A. Marquina, J. A. Font, and J. M. Ib'a nez Denoising of gravitational-wave signal GW150914 via total-variation methods





## Chirp Mass:

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{M^{1/5}} \simeq \frac{c^3}{G}$$

$$\frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^3$$

/5



1) HERE the consideration uses ONLY POINT PARTICLES NOT BH 2) Newton gravity Is not able to explain observations, but **GR AND** modified theories can do this

 $M = m_1 + m_2$  f is the GW frequency, f is its time derivative

BH NR fitting formula:

$$\begin{split} M\,\omega \ &= \ \frac{1}{8}\tau^{-3/8} \Big\{ 1 + \left(\frac{743}{2688} + \frac{11}{32}\nu\right)\tau^{-1/4} - \frac{3}{10}\pi\tau^{-3/8} \begin{array}{l} \text{At present there is NO} \\ \text{analogous formula} \\ &+ \left(\frac{47}{40}\frac{S_\ell}{M^2} + \frac{15}{32}\frac{\delta M}{M}\frac{\Sigma_\ell}{M^2}\right)\tau^{-3/8} \\ &+ \left(\frac{1855099}{14450688} + \frac{56975}{258048}\nu + \frac{371}{2048}\nu^2\right)\tau^{-1/2} + \left(-\frac{7729}{21504} + \frac{13}{256}\nu\right)\pi\tau^{-5/8} \\ &+ \left[\left(\frac{101653}{32256} + \frac{733}{896}\nu\right)\frac{S_\ell}{M^2} + \left(\frac{7453}{7168} + \frac{347}{896}\nu\right)\frac{\delta M}{M}\frac{\Sigma_\ell}{M^2}\right]\tau^{-5/8} \\ &+ \left(-\frac{720817631400877}{288412611379200} + \frac{53}{200}\pi^2 + \frac{107}{280}C - \frac{107}{2240}\ln\left(\frac{\tau}{256}\right) \\ &+ \left[\frac{25302017977}{4161798144} - \frac{451}{2048}\pi^2\right]\nu - \frac{30913}{1835008}\nu^2 + \frac{235925}{1769472}\nu^3\right)\tau^{-3/4} \\ &+ \left(-\frac{188516689}{433520640} - \frac{97765}{258048}\nu + \frac{141769}{1290240}\nu^2\right)\pi\tau^{-7/8}\Big\}, \end{split}$$

 $\tau = \nu (t_c - t)/5M$ ,  $\nu = \mu/M$ ,  $\mu = m_1 m_2/M$ ,  $\delta M = m_1 - m_2$  $t_c$  is the time at which the orbital-frequency diverges,  $\Sigma \equiv M \left[\frac{\mathbf{S}_2}{m_2} - \frac{\mathbf{S}_1}{m_1}\right]$ ,  $\mathbf{S} \equiv \mathbf{S}_1 + \mathbf{S}_2$ 

### Tests of general relativity with GW150914:



#### Fermi GBM Observations of LIGO Gravitational Wave event GW150914 arXiv:1602.03920



The LIGO localization map (top left) can be combined with the GBM localization map for GW150914-GBM (top right) assuming GW150914-GBM is associated with GW event GW150914. The combined map is shown (bottom left) with the sky region that is occulted to Fermi removed in the bottom right plot. The constraint from Fermi shrinks the 90% condence region for the LIGO localization from 601 to 199 square degrees.

The observed time-delay of GW150914 between the Livingston and Hanford observatories was 6.9<sup>+0.5</sup><sub>-0.4</sub> ms. With only the two LIGO instruments in observational mode, GW150914's source location can only be reconstructed to approximately an annulus set to first approximation by this time-delay.

## Interferometers - international network 'Simultaneously' detect signal (within msec)



## Alternative explanations of GW150914

C. Chirenti and L. Rezzolla: Did GW150914 produce a rotating gravastar?

arXiv:1602.08759



## S.Bird, I.Cholis, J. B. Munoz, Y.Ali-Haimoud, M. Kamionkowski, E. D. Kovetz, A. Raccanelli, and A. G. Riess: *Did LIGO detect dark matter?* arXiv:1603.00464

PBH mergers are likely to be distributed spatially more like dark matter than luminous matter and have no optical nor neutrino counterparts. They may be distinguished from mergers of BHs from more traditional astrophysical sources through the observed mass spectrum, their high ellipticities, or their stochastic gravitationalwave background.

## R.Konoplya, and A. Zhidenko: Detection of gravitational waves from black holes: Is there a window for alternative theories? arXiv:1602.04738

Here we shall show that this indeterminacy in the range of the black-hole parameters allows for some not negligible deformations of the Kerr spacetime leading to the same frequencies of black-hole ringing. This means that at the current precision of the experiment there remain some possibilities for alternative theories of gravity.

#### Problems in investigation of the tail of event GW150914 and QNM



V.Cardoso, E.Franzin, P. Pani: *Is the gravitational-wave ringdown a probe of the event horizon?* arXiv:1602.07309

If the final object is a BH, the ingoing condition at the horizon simply takes the ringdown waves and "carries" them inside the BH. In this case, the BH QNMs incidentally describe also the ringdown phase.

However, if the horizon is replaced by a surface of different nature (as, e.g., in the gravastar or in the firewall proposals) the relaxation of the corresponding horizonless compact object should then consist on the usual light-ring ringdown modes (which are no longer QNMs), followed by the proper modes of vibration of the object itself.

### The Time, Energy and Temperature scales in the Universe

t	$ ho^{1/4}$	Т	Event
$10^{-42}$ s	10 <sup>18</sup> GeV	~ 0	Inflation begins ?
$10^{-36\pm 6} s$	10 <sup>13±3</sup> GeV	~ 0	Inflation ends, Cold Big Bang starts?
10 <sup>−18±6</sup> s	$10^{6\pm3}$ GeV	$10^{6\pm3}$ GeV	Hot Big Bang begins ?
$10^{-10} s$	100 GeV	100 GeV	Electroweak phase transition ? (LHC)
$10^{-4} s$	100 MeV	100 MeV	Quark-hadron phase transition? (NICA)
$10^{-2} s$	10 MeV	10 MeV	γ, ν, e <sup>∓</sup> , n, p in thermal equilibrium
1 s	1 MeV	1 MeV	v decoupling, $e^{\mp}$ annihilation
100 s	0.1 MeV	0.1 MeV	Nucleosynthesis
10 <sup>4</sup> yr	1 eV	1 eV	Matter-radiation equality
10 <sup>5</sup> yr	0.1 eV	0.1 eV	Atom formation, photon decoupling
$\sim~10^9~{ m yr}$	$10^{-3}$ eV	$10^{-4}$ eV	First bound structures forms
Now	$3 \times 10^{-3}$ $h^{1/2} (0_{\circ})^{1/4} e^{1/4}$	2.72548 ± 0.00057 K	The present state of Universe

## **Some Conclusions**

1. The GW150914 confirms the existence of some kind of GW at the 5.1 sigma level !

2. The absence of data about polarization of the GW in GW150914 does not permit us to distinguish GR from modified theories of gravity and to confirm validity of GR.

3. The basic hypothesis in the analysis of GW150914 – the validity of GR can not be true, since we know that GR plus Standard Particle Model are not enough to describe NATURE, and one needs peremptorily:

a) To introduce DARK ENERGY and DARK MATTER, which leads to possibility for alternative explanations of GW150914, or:

b) To consider modified theories of gravity which are able to give their own alternative explanations of GW150914. At present the modified theories are not developed enough.

4. The presence of BH in GW150914 is not well substantiate and follows from preliminary assumptions during the analysis of data! Actually, the GW150914 leads to a crisis in the theory of BH, because masses about 30-60 solar masses are not compatible with the evolution of the known stars.

5. The old theory ('60) of the gravitational collapse must be reconsidered to take into account modern knowledge of matter EOS. The very theory of EOS is not complete and firmly establish.

5. A further analysis of the real data without any preliminary physical hypotheses is needed.

7. Only the analysis of QNM in the GW150914 tail may give us undisputable information about the nature of the final remnant. This is not done at present.

